

Express Mail Label No. EV 331074749 US

**ILLUMINANT-NEUTRAL GRAY COMPONENT REPLACEMENT IN SYSTEMS FOR  
SPECTRAL MULTIPLEXING OF SOURCE IMAGES TO PROVIDE A COMPOSITE  
IMAGE, FOR RENDERING THE COMPOSITE IMAGE, AND FOR SPECTRAL  
DEMULTIPLEXING OF THE COMPOSITE IMAGE**

**CROSS-REFERENCE TO RELATED APPLICATIONS**

[0001] Cross-reference is made to the following co-pending and commonly-owned applications, the disclosures of which are incorporated herein by reference:

[0002] U.S. Appln. No. 10/268,333, filed 10/09/2002 by Gaurav Sharma et al. and respectively entitled "Systems for spectral multiplexing of source images to provide a composite image, for rendering the composite image, and for spectral demultiplexing of the composite image" (Attorney Docket No. D/A1458).

[0003] U.S. Appln. No. 10/304,171 filed 11/25/2002 by Gaurav Sharma et al. and respectively entitled "Systems for spectral multiplexing of source images to provide a composite image, for rendering the composite image, and for spectral demultiplexing of the composite image by use of an image capture device" (Attorney Docket No. D/A1458Q).

[0004] U.S. Appln. No. 10/268,394 filed 10/09/2002 by Steven J. Harrington et al. and respectively entitled "Systems for spectral multiplexing of source images to provide a composite image, for rendering the composite image, and for spectral demultiplexing of the composite image to animate recovered source images" (Attorney Docket No. D/A1449).

[0005] U.S. Appln. No. 10/268,295 filed 10/09/2002 by Steven J. Harrington et al. and respectively entitled "Systems for spectral multiplexing of source images

including a stereogram source image to provide a composite image, for rendering the composite image, and for spectral demultiplexing of the composite image" (Attorney Docket No. D/A1449Q).

[0006] U.S. Appln. No. 10/268,505 filed 10/09/2002 by Steven J. Harrington et al. and respectively entitled "Systems for spectral multiplexing of source images including a textured source image to provide a composite image, for rendering the composite image, and for spectral demultiplexing of the composite image" (Attorney Docket No. D/A1449Q1)

[0007] U.S. Appln. No. 10/268,575, filed 10/09/2002 by Gaurav Sharma et al. and respectively entitled "Systems for spectral multiplexing of source images to provide a composite image with gray component replacement, for rendering the composite image, and for spectral demultiplexing of the composite image" (Attorney Docket No. D/A2228)

[0008] U.S. Appln. No. 10/268,246 filed 10/09/2002 by Robert P. Loce et al. and respectively entitled "Systems for spectral multiplexing of a source image and a background image to provide a composite image, for rendering the composite image, and for spectral demultiplexing of the composite images" (Attorney Docket No. D/A2229).

[0009] U.S. Appln. No. 10/268,271 filed 10/09/2002 by Yeqing Zhang et al. and respectively entitled "Systems for spectral multiplexing of source images to provide a composite image, for rendering the composite image, and for spectral demultiplexing the composite image, which achieve increased dynamic range in a recovered source image" (Attorney Docket No. D/A2230).

[0010] U.S. Appln. No. 10/268,241 filed 10/09/2002 by Yeqing Zhang et al. and respectively entitled "System for spectral multiplexing of source images to provide a composite image with noise encoding to increase image confusion in

the composite image, for rendering the composite image, and for spectral demultiplexing of the composite image" (Attorney Docket No. D/A2230Q).

### **FIELD OF THE INVENTION**

[0011] The present invention relates to a system or systems for spectrally multiplexing a plurality of source images so as to provide a composite image, rendering the composite image, and demultiplexing of such a composite image to recover one or more of the source images.

### **BACKGROUND OF THE INVENTION**

[0012] Whereas light sources are visible by their own emitted light, objects and materials appear to the eye according to how they modify incident light. The sensation of the color of an object is evoked by the physical stimulation of light-sensitive receptors in the human retina. The stimulation consists of electromagnetic radiation in the visible spectrum comprising wavelengths between about 380 and 780 nanometers.

[0013] Perceived color of the object is the result of a combination of factors, such as: (1) the spectral power distribution of an illuminant emitted by a light source that is incident upon the object, (2) the modification of the spectral power distribution of the illuminant by the spectral reflectance or transmission characteristics of the illuminated object, (3) the excitation of light sensitive receptors in the eye by the modified light from the object, and (4) the perception and interpretation by the brain of signals produced by the light sensitive receptors.

[0014] The perception of color is attributed to the differing spectral sensitivities of the light sensitive receptors. The trichromacy of color sensation implies that many different spectral distributions can produce the same perceived color. Such equivalent stimuli, which produce the same perception even though they are

physically different spectral distributions, are called metamers, and the phenomena metamerism. For example, it is known that the perceived color of an object can change quite markedly when the object is moved from incident daylight into incident artificial light. The spectrum of the illuminating light source is also known to have an effect on the perceived colors of a printed image in spite of the considerable physiological compensation that the eye makes for differences in illumination. Light sources of differing relative spectral power distributions are therefore known to have different color rendering properties: for example, light sources which emit very narrow-band, or almost monochromatic, light are considered to render colors very poorly.

[0015] According to the concept of metamerism, the respective colors of two objects may appear to be identical even though typically the spectral power distributions produced from the objects are different. Such power distributions, or stimuli, which are spectrally different but visually identical, are considered as metameric pairs. Because we measure light using only three cone types, the differences in these power distributions are indistinguishable. Two objects with different spectral reflectance functions may be perceived to match in color under one illuminant and not match under a different illuminant.

[0016] Certain aspects of perceived color have been employed to disguise images by printing an image in one color and then overprinting the first image with a pattern in a different color having approximately the same apparent brightness. Adjacent zones of equal brightness appear to be visually blended, even though they are of differing colors, thereby confusing the perception of the original image.

[0017] It is known to print patterns in different colors such that the patterns may be viewed through one or more filters having certain correlated colors, such that the patterns will change, depending upon the colors involved. It is also known to print characters in different colors in an overlapping relationship such that the overlapped characters, when viewed through one colored filter, will give the

appearance of only certain ones of the superimposed characters, and when viewed through a second and differing colored filter, will reveal certain other ones of the superimposed characters. Such approaches are known for encoding (or encrypting) information to prevent recognition of the information content of the pattern until the pattern is decoded and made comprehensible. These approaches have been applied to promotional gaming technology and in document security and document verification applications.

[0018] Techniques are known for rendering flat, two-dimensional images that can stimulate an illusion of depth perception, that is, of a three-dimensional object or scene. Devices for performing binocular stereoscopic imaging include binocular viewers, parallax stereograms, lenticular-sheet binocular stereoscopic pictures, and binocular displays using Polaroid glasses or color filters. Devices for performing autostereoscopy include parallax panoramagrams, lenticular-sheet three-dimensional imaging, projection type three-dimensional displays, and integral photography. Anaglyphic stereoscopy is a well-known process, in which left and right nearly-identical images are color-encoded by use of respective complementary color filters (e.g. cyan and red) for subsequent viewing through correspondingly colored lenses to separate the images as necessary for a simulated three-dimensional effect. When viewed through colored spectacles, the images merge to produce a stereoscopic sensation. The encoded image pair is known as an anaglyph, as it is typically rendered as two images of the same object taken from slightly different angles in two complementary colors.

## **SUMMARY OF THE INVENTION**

[0019] Spectral multiplexing, as used herein, refers to a process for encoding plural source images in a composite image. Composite image rendering refers to a process for rendering the composite image in a physical form. Spectral demultiplexing refers to a process for recovering at least one of the encoded

source images from the rendered composite image, such that the recovered source image is made distinguishable from, or within, the composite image, by subjecting the rendered composite image to at least one illuminant having a defined spectral energy distribution that is selected to reveal the source image.

[0020] Accordingly, the present invention is directed to methods and apparatus for spectrally-encoding plural source images and for providing the spectrally-encoded plural source images in a composite image, for rendering the composite image in a physical form, and for recovering at least one of the encoded source images from the rendered composite image such that the recovered source image is made distinguishable. For example, when the rendered composite image is subjected to an illuminant having a predefined spectral power distribution for which a source image was encoded, the source image becomes visually detectable by an observer.

[0021] A given source image is spectrally encoded by mapping values representative of each source image pixel to a corresponding pixel value in one or more of a plurality of colorant image planes. The composite image may be defined in a spectrally multiplexed (SM) image plane, which may have any number of different patterns of pixels, with a primary characteristic being that the SM image plane is spectrally multiplexed. In general, at each location in the SM image plane, a pixel value representing one or more spectral components may be present, and which spectral component is present depends on the gray level of the corresponding pixel in one of the separation image planes that described the source image. Alternatively, the SM image planes may be spectrally multiplexed in which each pixel includes color values representative of color separation image data from more than one source image plane.

[0022] Plural monochromatic separation images may be designed to be combined in the composite image, which in turn will control the amount of one or more colorants to be deposited on the substrate. For example, each colorant may

be assigned to a respective colorant image plane of the composite image, and the colorant values in the respective colorant image planes represent the relative amounts of colorant deposited in the rendered composite image. A rendered composite image may be rendered using colorants, such as cyan, magenta, yellow, and black, that are selectively deposited over a given area on a substrate by a rendering device.

[0023] A composite image composed of the plural colorant image planes may be stored or transmitted as a composite image file. The composite image may then be physically realized by delivering the composite image file to a rendering device with instructions for rendering the composite image on a substrate using the identified colorant or array of colorants. One suitable embodiment of a rendering device therefore includes a digital color electrophotographic printer.

[0024] In another embodiment of the contemplated encoding, the mapping of each source image is performed according to determinations described herein for compensating the effect of one or more of the following on the composition, rendering, or demultiplexing of the composite image: (a) the trichromacy of human visual response to colorant/illuminant interaction; (b) the spectral characteristics of the colorants selected for rendering the composite image, such spectral characteristics especially comprehending the interaction of plural colorants when such are combined on the substrate, and (c) the spectral characteristics of the narrow-band illuminant(s) that will be used to illuminate the composite image for recovering the source image(s).

[0025] It will no doubt be appreciated that the encoding of a source image in the composite image may be accomplished according to the teachings herein with use of either software, hardware or combination software-hardware implementations.

[0026] Accordingly, the present invention is directed to a system for spectrally-encoding plural source images and for providing the spectrally-encoded plural source images in a composite image.

[0027] The present invention is also directed to a system for rendering the composite image on a substrate. The composite image may be realized as a single, complex, rendered pattern of deposited colorants, wherein at least one colorant is utilized for its particular spectral reflectance characteristic, and in particular for its narrowband absorption characteristic.

[0028] The present invention is also directed to a system for spectral demultiplexing of one or more source images encoded in a rendered composite image. A source image may be recovered when the rendered composite image is subjected to illumination by an complementary illuminant having a selected spectral power distribution for which the source image was encoded.

[0029] In one embodiment of the invention, a source image in a rendered composite image may be recovered when the composite image is illuminated by a controlled field of illumination of at least one illuminant having a selected narrowband spectral power distribution.

[0030] In another embodiment of the invention, source image data representative of a plurality of disparate, pictorial source images may be spectrally encoded to form secondary image data representative of a composite image. The composite image may be realized as a single, complex, rendered pattern of deposited colorants, wherein at least one colorant is utilized for its particular spectral reflectance characteristic, and in certain embodiments, for its narrowband absorption characteristic. The source images are accordingly spectrally multiplexed to provide a composite image which is recorded on the substrate by use of at least one of the narrowband-absorbing colorants.



[0031] Typically, with respect to a composite image having encoded therein at least two source images, at least one of the first and second source images is not easily recognized as such while the rendered composite image is subject to a wideband illumination condition such as ambient white light. That is, until the rendered composite image is subjected to the spectral demultiplexing process, the rendered composite image is, to a certain extent, visually confused such that an observer is substantially unable to discern one or more of the source images by unaided viewing of the rendered composite image. Alternatively, one or more of the source images may be encoded so as avoid or reduce visual confusion in the rendered composite image during the wideband illumination condition, and therefore be more visible in the rendered composite image when the rendered composite image is subjected to ambient white light or similar wideband illuminant, and so as to become confused or difficult to detect when the rendered composite image is subjected to a complementary illuminant.

[0032] In another embodiment of the invention, a colorant selected for its narrowband absorbing properties may be employed to appear dark when subjected to its complementary narrowband illuminant, and to appear light when subjected to a differing illuminant having a spectral power distribution that lies substantially outside of the spectral absorption band of the particular colorant. For example, a cyan colorant may be selected for its absorption of red light, and accordingly the regions of a rendered composite image that are composed of a cyan colorant will exhibit high darkness under red light. The cyan colorant will exhibit low darkness under blue light, and will exhibit intermediate darkness under green light. Likewise, a magenta colorant will exhibit high darkness under green light, low darkness under red light, and an intermediate darkness under blue light. A yellow colorant will exhibit high darkness under blue light, low darkness under red light, and an intermediate darkness under green light.

[0033] In another embodiment of the present invention, by using cyan, magenta, and yellow colorants and complementary illuminants having respective spectral distributions in the red, green, and blue regions of the visible spectrum, respective source images may be encoded and rendered using each of the respective colorants, and each of the corresponding source images are distinguishable within the rendered composite image when the rendered composite image is subjected to illumination by a complementary illuminant.

[0034] An embodiment of the system for spectral multiplexing of plural source images includes a spectral multiplexer for receiving image data representative of a plurality of source images and for processing the image data to encode the plurality of source images into a composite image data signal. One embodiment of the spectral multiplexer may be provided in the form of a computer for receiving image data files representative of a plurality of source images and for encoding the image data files as a composite image data file, and a composite image file storage and/or transmission means connected to the computer.

[0035] An embodiment of the system for rendering the composite image includes an image recording device which is responsive to the system for spectral multiplexing for receiving the composite image data file and for rendering the corresponding composite image on a substrate. One embodiment of the image recording device may be provided in the form of a printer connected to the composite image file storage and/or transmission means, for printing the composite image on a substrate. An embodiment of the printer may include colorants in the form of cyan, magenta, yellow, and black pigments, inks, or dyes selected for their apparent darkness when exposed to complementary illuminants.

[0036] An embodiment of the system for spectral demultiplexing of a rendered composite image may include a spectral demultiplexer for subjecting the rendered composite image to an incident light spectrum having a selected spectral power distribution in at least one of three selectable bands of radiant energy. In a typical

embodiment, such selectable bands are contemplated as corresponding to the long, medium, and short (LMS) wavelength bands of the visible light spectrum. Accordingly, a first mode of operation of the spectral demultiplexing may be employed to subject the rendered composite image to a first illuminant respectively exhibiting a spectral power distribution located in a first one of the three wavelength bands, such that at least one recovered image (representing a first source image) is recovered to form a normalized color image. A second, optional, mode of operation of the spectral demultiplexing will subject the rendered composite image to a second illuminant exhibiting a spectral power distribution located in a remaining other one of the three wavelength bands, such that a second source image is recovered.

[0037] The spectral demultiplexer may include an illuminant source responsive to manual control, or a controller and an illuminant source responsive to control by illuminant source control signals provided by the controller. An embodiment of the illuminant source may include one or more light sources for providing desired spectral power distributions in single or plural selectable bands of radiant energy. In certain embodiment, three selectable bands of radiant energy are provided which correspond to predefined spectral power distributions in the red, green, and blue regions of the visible spectrum.

[0038] An embodiment of the controller may include a computer, operable according to control programs for generating one or more of the illuminant source control signals, and an illuminant source responsive to the illuminant source control signals for generating a defined field of illumination of narrowband illuminant, whereby a rendered composite image on a substrate may be located within the field of illumination and thereby subjected to illumination by one or more illuminants that exhibit the desired spectral power distributions.

[0039] A rendered composite image, when subject to a wideband illumination condition such as ambient white light, may exhibit visual confusion, that is, the

appearance of the rendered composite image lacks, to a certain extent, perceptible resemblance to one or more of the source images encoded therein.

[0040] In certain embodiments of the present invention, it may be desirable for the rendered composite image, when subjected to a wideband illumination condition, to appear visually confused to a selectable extent. Accordingly, the present invention is directed to methods and apparatus for controlling visual confusion in a rendered composite image.

[0041] In an embodiment of the invention, an illuminant-neutral gray component replacement technique may be applied to the apparent darkness common to the colorants in a rendered composite image. This illuminant-neutral GCR technique is generally described and taught herein as being considered to include the technique of replacing a given colorant with a selected non-neutral colorant, or a mixture of selected neutral and non-neutral colorants.

[0042] The neutrality of the replacement colorant is illuminant-dependant; for example, to increase visual confusion, embodiments of the modified illuminant-neutral GCR technique typically employ a replacement colorant that is non-neutral under white light and neutral under a selected one or more of complementary illuminants.

[0043] Accordingly, use of this illuminant-neutral GCR technique in the encoding and rendering of a composite image can advantageously effect a selective amount of visual confusion in the rendered composite image when the rendered composite image is subject to a wideband illumination condition such as ambient white light. Selective use of a non-neutral replacement colorant in a rendered composite image can effect greater visual confusion in the rendered composite image (when under white light) than would otherwise be obtained by the use of a neutral replacement colorant such as black. This is due to the high density of black colorant under wideband illumination conditions. Hence, a

replacement colorant that is non-neutral under wideband illumination conditions should exhibit significantly less density in such conditions.

[0044] In another embodiment of the invention, a fractional GCR component (*frac*) used in the contemplated illuminant-neutral GCR technique can be spatially modulated, so as to effect a spatial variation in the extent of visual confusion in the rendered composite image.

[0045] In another embodiment of the invention, a gray component replacement fraction used in the illuminant-neutral GCR technique may be spatially modulated, so as to encode a respective source image in the rendered composite image for recovery in a wideband illumination condition such as ambient white light. For example, the fractional GCR component (*frac*) can have an imagewise spatial dependence according to the desired source image. When the resulting rendered composite image is subjected to white light illumination, the desired image is visually discernible.

[0046] An advantage realized in certain embodiments of this illuminant-neutral GCR in the encoding and rendering of a composite image will include an increase in the dynamic range of the images recovered from the rendered composite image.

### **BRIEF DESCRIPTION OF THE DRAWINGS**

[0047] The patent or application file contains at least one drawing executed in color. Copies of this patent or patent application publication with color drawing(s) will be provided by the Office upon request and payment of the necessary fee.

[0048] Figure 1 represents reflectance spectra for a white paper substrate and colorants in the form of Cyan, Magenta, Yellow, and Black dyes (at 100% density) operable in a dye sublimation printer.

[0049] Figure 2 represents the relative radiance spectra for the red, green, blue primaries generated by a typical cathode ray tube (CRT).

[0050] Figure 3 is a block diagram of systems for spectral multiplexing and demultiplexing of plural source images, and for rendering a composite image having therein at least one encoded source image, constructed according to the invention.

[0051] Figure 4 is a simplified schematic diagram of methods operable in the system of Figure 3 for spectrally multiplexing first and second source images in a composite image, rendering the composite image with use of at least two colorants, and for demultiplexing the rendered composite image.

[0052] Figure 5 is a schematic simplified representation of the spectral multiplexing system of Figure 3, in which an image processing unit and associated peripheral devices and subsystems are employed.

[0053] Figure 6 is a simplified schematic representation of the spectral demultiplexing system of Figure 3, in which a controller and associated peripheral devices and subsystems are employed.

[0054] Figure 7 is a schematic representation of a rendered composite image illustrating the dominance of a cyan image when subjected to illumination by white light.

[0055] Figure 8 is a schematic representation of a rendered composite image illustrating the operation of gray component replacement (GCR) in the production of a rendered composite image, wherein the density of a cyan image when subjected to white light may be increased in comparison to the density of the cyan image when subjected to red light.

[0056] Figure 9 is a rendered composite image, wherein first and second source images were encoded in a composite image and the composite image was rendered in cyan and yellow colorants, wherein the first and second source

images are intended for subsequent recovery when subjected to red and blue illuminants, respectively.

[0057] Figure 10 is a rendered composite image created with a K-based 80% GCR fraction,

[0058] Figure 11 is a rendered composite image created with an illuminant-neutral GCR technique that is considered illuminant-neutral.

[0059] Figure 12 is a rendered composite image created with an illuminant-neutral GCR technique that is considered illuminant-neutral, wherein a third source image is included for recovery under an ambient wideband light condition, such as white light.

[0060] Figure 13 is a rendered composite image created with an illuminant-neutral GCR technique that is considered illuminant-neutral, wherein square blocks of pixels in the composite image are subject to a random variation in the illuminant-neutral GCR.

[0061] Figure 14 is a rendered composite image created with an illuminant-neutral GCR technique that is considered illuminant-neutral, using multiple colorants and a single monochromatic image.

## **DETAILED DESCRIPTION OF THE EMBODIMENTS**

### **Definition of Terms**

[0062] Color - A color can be uniquely described by three main perceptual attributes: hue, denoting whether the color appears to have an attribute according to one of the common color names, such as red, orange, yellow, green, blue, or purple (or some point on a continuum); colorfulness, which denotes the extent to

which hue is apparent; and brightness, which denotes the extent to which an area appears to exhibit light. Light sources used to illuminate objects for viewing are typically characterized by their emission spectrum and to a reduced degree by their color temperature, which is primarily relevant for characterization off sources with a spectrum similar to a black body radiator. See, for instance, Hunt, R. W. G., *Measuring Colour*, Ellis Horwood, 1991, and Billmeyer and Saltzman, *Principles of Color Technology, 3rd Ed.* (Roy S. Berns), John Wiley & Sons, 2000.

[0063]            Chroma - Colorfulness of an area judged as a proportion of the brightness of a similarly illuminated area that appears white or transmitting.

[0064]            Colorant - A dye, pigment, ink, or other agent used to impart a color to a material. Colorants, such as most colored toners, impart color by altering the spectral power distribution of the light they receive from the incident illumination through two primary physical phenomenon: absorption and scattering. Color is produced by spectrally selective absorption and scattering of the incident light, while allowing for transmission of the remaining light. A narrowband (absorbing) colorant exhibits an absorption band that is situated in a substantially narrow region of the visible region of the spectrum. Cyan, magenta and yellow colorants are examples of narrowband colorants that selectively absorb red, green, and blue spectral regions, respectively. Some colorants, such as most colored toners, impart color via a dye operable in transmissive mode. Other suitable colorants may operate in a reflective mode.

[0065]            Composite Image - An array of values representing an image formed as a composite of plural overlaid (or combined) colorant image planes. Source images may be encoded as described herein and the resulting image planes are combined to form a composite image. When a rendered composite image is subjected to a complementary illuminant having a selected spectral power distribution, the combined density of all colorants in the rendered composite image will reveal at least one source image that is otherwise difficult to



distinguish, or the reverse, depending upon the interaction of the specific colorant and its complementary illuminant.

[0066] Density (Optical) - The degree of darkness of an image. Higher density values represent greater darkness. Mathematically, optical density is defined as the negative logarithm of the reflectance or transmittance. The spectral density is correspondingly the negative logarithm of the reflectance/transmittance spectrum.

[0067] Hue - Attribute of visual sensation according to which an area appears to be similar to one of the perceived colors: red, green, yellow, and blue, or to a combination thereof. An achromatic color is a perceived color devoid of hue and a chromatic color is a perceived color possessing a hue. See, for instance, Fairchild, Mark D., *Color Appearance Models*, Addison Wesley, 1998.

[0068] Gamut - A range of colors; typically, the range of colors that can be produced by a device.

[0069] Grayscale - Image data representing one of a series of tones stepped from light to dark.

[0070] Gray Component Replacement (GCR) - A technique whereby a replacement colorant is used to replace a portion of common darkness of other component colorants in printing an image.

[0071] Image - An image may be described as an array or pattern of pixels that are mapped in a two-dimensional format. The intensity of the image at each pixel is translated into a numerical value which may be stored as an array that represents the image. An array of numerical values representing an image is referred to as an image plane. Monochromatic or black and white (gray scale) images are represented as a two-dimensional array where the location of a pixel value in the array corresponds to the location of the pixel in the image. Multicolor (polychromatic) images are represented by multiple two-dimensional arrays. In a three color arrangement, each array represents one of the primary colors. In the

digital processing of color images, the individual color separations are represented as a digital image with a plurality of discrete elements ("pixels") defined by position and gray value. In such a system, gray value is described as one level in a number of possible states or levels. When more than two different levels are used in the description of an image, the levels are termed "gray" (without regard to the actual color) to indicate that the pixel value is between some maximum and minimum gray level.

[0072]            Illuminant - Incident luminous energy specified by its relative spectral power distribution; typically provided by a light source having a predefined spectral power distribution. A narrowband illuminant is an illuminant having a spectral power distribution that is substantially limited to a narrow region of the spectrum. The bandwidth of the region may vary from extremely narrow for a LASER source, to narrowband illuminants such as natural or artificial light transmitted through a band-limited color filter. Examples of red, green and blue light are shown in Figure 2, which illustrates the spectral power distributions obtained from activated red, green, and blue phosphors in a typical CRT. An illuminant that is designed to particularly interact with a given colorant is said to be complementary, and vice versa. A complementary illuminant typically exhibits a spectral power distribution that substantially corresponds to the spectral absorption band of a particular colorant.

[0073]            Image plane - A two-dimensional representation of image data. The uppercase letters C, Y, M, K are used herein to indicate two-dimensional arrays of values representing a monochromatic image or a separable component of a polychromatic (multicolor) image. Two-dimensional arrays of values may also be referred to as "planes." For example, the Y plane refers to a two-dimensional array of values that represent the yellow component at every location (pixel) of an image.

[0074]           Imaging Device - A device capable of generating, capturing, rendering, or displaying an image; including devices that store, transmit, and process image data. A color imaging device has the capability to utilize color attribute information.

[0075]           Lightness - The perceptual response to luminance; denoted  $L^*$  and is defined by the CIE as a modified cube root of luminance. Common notation indicates the lightness or darkness of a color in relation to a neutral grey scale, which extends from absolute black to absolute white.

[0076]           Neutral – A quality of a color that describes its lack of a predominant hue. Neutral colorants give rise to the perception of neutral colors when subjected to broadband white illumination. Examples of neutral colors are black, gray and white. Non-neutral refers to a color that exhibits a predominant hue. Non-neutral colorants give rise to the perception of non-neutral colors when subjected to a broadband white illumination. Examples of common non-neutral colorants are cyan, magenta and yellow.

[0077]           Primary Colors - Colors, usually three, which are combinable to produce a range of other colors within a color mixing model. All non-primary colors are mixtures of two or more primary colors. Red, green, and blue (R, G, B) are the standard additive primary colors. Cyan, magenta, and yellow (C,M,Y,K) are the standard subtractive primary colors. Black (K) colorant absorbs light energy substantially uniformly over the full extent of the visible spectrum and may be added to enhance color and contrast and to improve certain printing characteristics. Cyan, magenta, and yellow are the subtractive complements of red, green, and blue, respectively and they absorb the light energy in the long, middle, and short wavelength regions, respectively, of the visible spectrum, leaving other regions of the visible spectrum unchanged. Ideally, the absorption bands of individual CMY colorants are non-overlapping and completely cover the visible region of the spectrum. Actual CMY colorants do not satisfy these *block-*

dye assumptions; instead, their absorption spectra are smooth and include some unwanted absorptions in their transmission bands. The reflectance spectra for white paper and cyan, magenta, yellow, and black colorants (100%) from a dye-sublimation printer are shown in Fig. 1. Red, green, and blue are the additive complements of cyan, magenta, and yellow respectively.

[0078]            Saturation - Colorfulness of an area judged in proportion to its brightness. Saturation is judged for an area relative to its own brightness whereas chroma is judged relative to a similarly illuminated area that appears white.

[0079]            Subtractive Color Model The production of color wherein light is subtracted through a process such as absorption; a color model in which colors may be produced by combining various percentages of the subtractive primaries (cyan, magenta, and yellow).

### **Introduction to a General Theory of the Invention**

[0080]            Two predominant modes for producing color are: Additive color, whereby color is produced by the addition of spectrally selective lights to a dark background that is otherwise substantially devoid of light; and subtractive color, whereby color is produced by spectrally selective subtraction of light energy from the light emitted by a source. Red, green and blue lights are typically used as the primaries that are mixed together in an additive system. In a subtractive system, colorants are typically used as the subtractive primaries. These colorants selectively absorb, or subtract, a portion of the visible spectrum of incident light while transmitting the remainder. Cyan, magenta, and yellow colorants are typically used.

[0081]            Color in printed images results from the combination of a limited set of colorants deposited on a substrate over a small area in densities selected to integrate the desired color response. This is accomplished in many printing

devices by reproducing so called "separations" of the image, where each separation provides varying gray values of a single primary color. When the separations are combined together, the result is a full color image.

[0082] Colorants that are deposited on a reflective substrate, such as a paper sheet, will selectively transmit incident light in a first pass to the surface of the substrate whereupon the transmitted light is then reflected by the substrate and is again filtered by the colorants in a second pass, thus encountering additional selective absorption before being perceptible as a particular color by an observer. It is also common for colorants to possess a degree of scattering, and the color appearance of a colorant on a printed substrate is determined by the amount and types of the colorants present, and the combination of their absorption and scattering properties.

[0083] In embodiments of the invention, most colors in a subtractive color setting may be reproduced in an image by use of different proportions of cyan, magenta, and yellow colorants. Each of these colorants is characterized primarily by its absorption characteristics. An idealized cyan colorant, for instance, may be defined as having an absorption band over the wavelength interval of about 600-700nm, commonly referred to as red light, or the red region of the spectrum. Likewise, an idealized magenta colorant has an absorption band over the interval of about 500-600nm, commonly referred to as green light, or the green region of the spectrum; and an idealized yellow colorant has an absorption band over the interval of about 400-500nm, commonly referred to as blue light, or the blue region of the spectrum.

[0084] Thus, cyan, magenta, and yellow colorants absorb red, green and blue light, respectively. The idealized absorption bands for the cyan, magenta, and yellow colorants are referred to as the block-dye assumption. In reality, colorants exhibit significant deviations from this idealized behavior, including variations of absorption within the absorption band, extension of the absorption band beyond

the idealized limits, and scattering in the colorants. In particular, the absorption of light in a spectral region outside the main absorption band of a colorant (as, for example, demonstrated by absorption in the blue and red regions of the spectrum by a magenta colorant), is considered unwanted absorption. Among typical colorants used for CMYK printing, magenta demonstrates the most unwanted absorptions and yellow the least. The black colorant absorbs uniformly through the visible region of the spectrum and can be used as a replacement for combined CMY for reasons of economy and improved rendition of dark regions.

[0085] Thus, according to the subtractive principle, a surface layer of a substrate such as a sheet of white paper, on which one can vary the concentrations of a cyan, a magenta, and a yellow colorant, thereby offers the means of varying the intensities of the reddish, greenish, and bluish parts of the white light reflected from the paper. To produce a subtractive color image reproduction, one can control the concentrations of the three colorants independently at localized areas on the paper substrate.

[0086] All surfaces, whether of a colorant or substrate, reflect from their topmost layer a certain proportion of the incident light which is added to that reflected from the body of the surface. This light reflected from the topmost layer is the same color as the illuminant, and therefore when a color surface is viewed in white light, some of the white light is added to the colored light reflected from the body of the surface and the colorfulness is therefore reduced. Most surfaces also exhibit some degree of gloss, and this means that, if the lighting is directional, the white light reflected from the topmost layer of the surface will be confined chiefly to a single direction, thus altering the appearance of the image to some extent depending on the angles of viewing and illumination.

[0087] Under normal viewing illumination, the eye adapts to the *white-point*, which usually corresponds to blank paper with the highest reflectance and different colors can be seen by the eye for prints made with different colorant

combinations. However, under relatively narrowband illumination, such as that obtained from a phosphor excited by a single gun of a CRT monitor, the eye is unable to distinguish color. Images viewed under narrowband illumination therefore appear to have only varying levels of gray and little or no chroma. Since the absorption characteristics of each of a plurality of colorants will differ in different spectral bands, the respective reflectance (or density) of each colorant when subjected to a series of differing narrowband illuminants will also appear to have varying levels of gray.

[0088] Embodiments of the present invention accordingly exploit the interaction between certain narrowband illuminants and their corresponding (complementary) colorants (especially the colorants typically used for printing), and the manner in which the eye detects images illuminated with illuminants having narrowband spectral power distributions. The methodology described herein may be generalized to apply to an arbitrary number of illuminants and colorants, and for the purpose of simplicity the invention is described with reference to the cyan, magenta, yellow, and black colorants commonly used in color printing applications, and to the narrow-band red, green, and blue illuminants commonly generated by CRT-based light sources. This description thus makes reference to the handling of monochromatic and polychromatic source images encoded according to an array of colorants such as the CMYK color primaries. However, it will be apparent to one of ordinary skill in the art that there are alternative spectral schemes to be employed in the spectral multiplexing of the invention. An alternative would include a color system that employs primary colorants other than CMYK for color representations, such as systems that use RGB primaries or high-fidelity colorants such as orange and green.

[0089] The general theory of the invention may be understood with reference to a rendering device in the form of a color hardcopy output device, such as a printer, and to a mathematical framework that employs nomenclature similar to

that used in conventional color imaging. Consider a color hardcopy output device with  $M$  colorants. Prints from this device are to be viewed under  $N$  different illuminants,  $\{L_i\}_{i=1}^N$ . The luminance characterization of the printer under the  $K$  viewing lamps is given by the relation between the control values  $\{A_j\}_{j=1}^M$  used for each of the  $M$  colorants at a given pixel location and the luminance produced at the given pixel location under each of the  $N$  illuminants. This can be denoted as the set of  $N$  functions, where  $i=1,2,\dots,N$ :

$$f_i(A_1, A_2, \dots, A_M) = \text{luminance of region} \\ \text{with colorant control values } A_1, A_2, \dots, A_M \text{ under } i\text{th illumination } L_i$$

[0090] In the following description, we assume that a control value of 0 for a given colorant represents no printing of that colorant. This convention is not a requirement in the practice of the invention and is only adopted for notational simplicity.

$$f_i(A_1, A_2, \dots, A_M) = \text{luminance of region} \\ \text{with colorant control values } A_1, A_2, \dots, A_M \text{ under } i\text{th illumination } L_i$$

[0091] In the following description, we assume that a control value of 0 for a given colorant represents no printing of that colorant. This convention is not a requirement for the invention and is only adopted for notational simplicity. The following description is limited to the case of luminance characterization alone, because under narrowband illumination the eye primarily sees differences of luminance and is unable to distinguish most color differences. Note that luminance as described here agrees in concept with its standard usage, i.e., as a measure of the perceived light energy; however, its definition is not limited to the conventional usage and is expanded to comprehend the special viewing situations also described herein. In particular, under narrowband illumination, specific visual effects may influence the perception of a source image. A specific instance of this is the Purkinje effect that causes increased sensitivity in the blue



region of the spectrum at low light levels, which may be of particular relevance for viewing under blue light and CRT illumination in general. Some of the advanced concepts from photometry and colorimetry that are required in such situations are described for instance in G. Wyszecki and W.S. Stiles, *Color Science: Concepts and Methods, Quantitative Data and Formulae, 2<sup>nd</sup> Edition*, John Wiley and Sons (1982).

[0092] The methods of the present invention are directed to the multiplexing, rendering, and recovery via demultiplexing of a source image encoded in a composite image. We assume that the one or more source images to be recovered are described by the spatial luminance distributions desired under each of the illuminants (although, in the alternative, any other equivalent specification that can be transformed to luminance/density may be used.) Thus, there are  $N$  images specified, with  $Y_i(x, y)$  being the desired luminance values that we wish to produce under the  $i$ th illuminant  $L_i$  where  $x, y$  denote the two spatial coordinates. For the purposes of simplifying the notation in the following discussion, the spatial dependence is sometimes dropped in the following description with the understanding that the discussion applies to each pixel location independently.

[0093] To examine the basic methodology symbolically, consider a simplified example of a composite image rendered in cyan and yellow colorants. In the simplified example below, additivity of "RGB" densities is assumed. This is for the purposes of simple illustration of the principles only and not intended to restrict the invention; in those situations where this approximation is invalid, more precise assumptions can be made. In this example: C, M, Y, K and R, G, B will respectively denote the colorants and illuminants; a superscript will denote illuminant; and a subscript will denote a colorant. Let:

[0094]  $d^R$  = density of the image perceived under R illumination,

[0095]  $d^B$  = density of the image under B,

[0096]  $d_C^R$  = density C separation under R,

[0097]  $d_C^B$  = density C separation under B,

[0098]  $d_Y^R$  = density Y separation under R,

[0099]  $d_Y^B$  = density Y separation under B.

[00100] When illuminated with a R or B illuminant, the total density perceived can be approximated as,

[00101]  $d^R(x, y) = d_C^R(x, y) + d_Y^R(x, y) \approx d_C^R(x, y)$

[00102]  $d^B(x, y) = d_C^B(x, y) + d_Y^B(x, y) \approx d_Y^B(x, y)$

[00103] Accordingly, this methodology exploits the characteristically low density of a colorant when subjected to a first illuminant having a predefined spectral power distribution and the characteristically high density exhibited by the same colorant when subjected to a second illuminant having a differing spectral power distribution. Thus, at least one perceptibly distinct source image (that is encoded in the rendered composite image by use of the particular colorant), can be imperceptible (or nearly so) to an observer when subjected to the first illuminant, but perceptibly distinguishable to the observer when illuminated by the second illuminant. Upon perception of the source image by an observer, the source image may be comprehended and the information embedded in the composite image, or the composite image itself, is thereby readily comprehended.

### **Determinations of Gamut Mapping, Dynamic Range, and Colorant Interaction**

[00104] The example presented above assumed that colorant interactions can be entirely ignored. This assumption is not true with most practical colorants and additional considerations are therefore required.

[00105] Consider the case of a rendered composite image that is produced by using C and M colorants for subsequent illumination under red and green illuminants. For simplicity, in our illustration below we assume additivity for the red, green, blue band densities, as the general case for situations where this approximation does not hold is described subsequently. A first source image may be recovered primarily from the cyan component of a composite image, and a second source image may be recovered primarily from the magenta component; however, unwanted absorption by these colorants are preferably compensated to avoid artifacts discernible by an observer. The total density under red illumination at pixel location (x,y) can be approximated as

[00106] 
$$d^R(x,y) = d_C^R(x,y) + d_M^R(x,y)$$

[00107] and the total density under green illumination is

[00108] 
$$d^G(x,y) = d_M^G(x,y) + d_C^G(x,y)$$

[00109] where  $d_U^V(x,y)$  represents the visual density under illuminant V due to colorant U at pixel location (x,y).

[00110] The terms  $d_M^R(x,y)$  and  $d_C^G(x,y)$  represent the unwanted absorption. In the simplest case, it can be assumed that a colorant's absorption under its complementary illuminant is used for two purposes: 1) to recover the desired image and 2) to compensate for unwanted absorption by the other colorant(s) present in the composite image. So a magenta colorant may be used to produce the desired image to be seen under green illumination and to compensate for the unwanted absorption of the cyan colorant; a cyan colorant may be used to produce the desired image under red illumination and to compensate for unwanted absorption of magenta under red illumination.

[00111] The portion that is used to compensate for the unwanted absorption should combine with the unwanted absorption to result in a constant spatial density so as to make the unwanted absorption imperceptible, or nearly so. Let

$d1_C^R(x,y)$  represent the portion of Cyan density that is used to compensate for the unwanted absorption of Magenta under red, which is determined by:

$$[00112] \quad d1_C^R(x,y) + d_M^R(x,y) = \text{constant} = q^R$$

[00113] The remaining density contribution of cyan under red illumination is  $d2_C^R(x,y) = d_C^R(x,y) - d1_C^R(x,y)$ . Note that the total density can be written in terms of these components as

$$[00114] \quad d^R(x,y) = d_C^R(x,y) + d_M^R(x,y) = d2_C^R(x,y) + (d1_C^R(x,y) + d_M^R(x,y))$$

$$[00115] \quad = d2_C^R(x,y) + q^R$$

[00116] Therefore the overall visual density under red illumination corresponds a constant background density of  $q^R$  with the spatially varying density pattern of  $d2_C^R(x,y)$  superimposed. This spatially varying pattern is the one that is seen under red illumination and should therefore represent the first multiplexed image that is to be seen under red illumination.

[00117] In a similar manner the density contribution of magenta under green illumination can be decomposed into a component  $d1_M^G(x,y)$  that is used to compensate for the unwanted absorption of cyan under green illumination, given by

$$[00118] \quad d1_M^G(x,y) + d_C^G(x,y) = \text{constant} = q^G$$

[00119] and the remaining component

$$[00120] \quad d2_M^G(x,y) = d_M^G(x,y) - d1_M^G(x,y)$$

[00121] which satisfies

$$[00122] \quad d^G(x,y) = d_M^G(x,y) + d_C^G(x,y) = d2_M^G(x,y) + d1_M^G(x,y) + d_C^G(x,y)$$

$$[00123] \quad = d2_M^G(x,y) + q^G$$

[00124] Therefore the overall visual density under green illumination corresponds to a constant background density of  $K^G$  with the spatially varying

density pattern of  $d_{2C}^R(x,y)$  superimposed. This spatially varying pattern is the one that is seen under red illumination and should therefore represent the second multiplexed image that is to be seen under green illumination.

[00125] Since the terms  $d_{2C}^R(x,y)$  and  $d_{2M}^G(x,y)$  represent the visual variations in density corresponding to the two multiplexed images, we would like to maximize their dynamic range. Since colorants can only add positive density, this requirement translates to minimizing the terms  $q^R$  and  $q^G$  subject to meeting the required equations and the physical constraint that colorants can only add positive density. We would therefore like to determine the smallest feasible values of  $q^R$  and  $q^G$  for which the above equations are feasible.

[00126] For the purpose of further illustration we use a first order approximation, that the amount of colorant added to compensate for unwanted absorption of the other colorant, itself only contributes a negligible amount of unwanted absorption (because of its small value). This assumption implies that the component of Magenta used to offset unwanted absorption of Cyan contributes negligibly to unwanted absorption under green and the component of Cyan used to offset unwanted absorption of Magenta contributes negligibly to unwanted absorption under blue. This assumption is used for illustration only, in practice, one can iteratively determine the appropriate amounts to account for higher-order effects or use an appropriate model or look-up table (LUT). With this simplifying assumption, the range achievable for the desired spatially varying pattern  $d_{2C}^R(x,y)$  under red illumination is between  $q^R$  and  $d_C^R(x,y)$  with a total density variation or dynamic range of  $d_C^R(x,y) - q^R$ . Likewise the total density range available under green illumination is  $d_M^G(x,y) - q^G$ .

[00127] One set of feasible values for the terms  $q^R$  and  $q^G$  can be determined as:

[00128]  $q^R = \max(d_M^R(x,y)) = d_M^R(255) = \text{max density for Magenta under red illuminant}$

[00129]  $q^G = \max(d_C^G(x,y)) = d_C^G(255) = \text{max density for Cyan under green illuminant}$

[00130] This can be thought of as follows: the background density under red light  $q^R$  is equal to the maximum unwanted density that one can have from Magenta. The Cyan density component  $d_C^R(x,y)$  is designed carefully so that the combination of Cyan and Magenta at each pixel has a density  $q^R$ , this can be achieved by putting no Cyan where Magenta is 100% (255 digital count) and appropriate amounts of Cyan to make up the density to  $q^R$  at pixels which have less than 100% Magenta. A similar argument applies to the Magenta density component  $d_M^G(x,y)$  that compensates for the unwanted absorption of Cyan under red illumination.

[00131] With the notation and terminology defined earlier, the general multi-illuminant imaging problem reduces to the following mathematical problem:

[00132] Given  $N$  luminance values  $\{Y_i\}_{i=1}^N$  corresponding to the desired luminance values under the  $N$  different illuminants, determine a set of control values for the  $M$  colorants  $\{B_j\}_{j=1}^M$  to be used in printing a pixel, such that for all  $i=1,2,\dots,N$ :

[00133] 
$$f_i(B_1, B_2, \dots, B_M) = \text{luminance of pixel under } i\text{th illumination } L_i = Y_i$$
  
(1)

[00134] Typically, for  $N > M$  (number of image specifications > number of colorants) the system is over-determined and has a solution only under severe constraints on the  $\{Y_i\}_{i=1}^K$  luminance values limiting its utility in illuminant multiplexed imaging. Even if  $N \leq M$  (number of image specifications  $\leq$  number of colorants), the system of  $N$  equations presented in (1) above has a solution

(corresponding to realizable device control values  $\{B_j\}_{j=1}^M$ ) only in a limited region of luminance values, which we refer to as the gamut for the spectrally multiplexed imaging problem:

$$\begin{aligned} G &= \text{gamut achievable for illuminant multiplexed imaging} \\ [00135] \quad &= \{ \mathbf{Y} \in R_+^K \text{ such that system (1) has a realizable solution} \} \\ (2) \end{aligned}$$

[00136] where  $\mathbf{Y} = [Y_1, Y_2, \dots, Y_N]$ , denotes the vector of luminance values under the  $N$  illuminants, and  $R_+$  is the set of nonnegative real numbers. For specified  $N$ -tuples of luminance values within the gamut  $G$ , there is a set of realizable control values such that a pixel printed with the control values produces the required luminance values under the given illuminants. Vice versa,  $N$ -tuples of luminance values outside the gamut  $G$  cannot be created using any realizable control values. The situation is analogous to the limited color gamut encountered in color reproduction. It is necessary to include a gamut mapping step in the spectral multiplexing described herein to ensure that the source images are limited to the gamut of the system before attempting to reproduce them. The gamut mapping may be image independent or image dependent, where the term image is used to imply the set of desired source images recoverable under the different illuminants. In addition, the set of images to be multiplexed may be designed to take into account the gamut limitations and produce the best results with those gamut limitations.

[00137] Once the source images to be multiplexed have been mapped to the achievable gamut  $G$ , the problem of reproduction reduces to the determination of the control values for each of the  $M$  colorants for each pixel. This corresponds to an inversion of the system of equations in (1) and in a manner similar to color calibration, the inverse could be pre-computed and stored in  $N$ -dimensional look-

up tables (LUTs), with one LUT one per colorant (or alternately, a single  $N$ -dimensional LUT with  $M$  outputs).

[00138] In practice, the function in (1) itself needs to be determined through measurements of the device response by printing a number of patches with different  $M$ -tuples of control values and measuring them suitably to obtain the luminance under the different illuminants. The full spectrum of the patches may be measured for instance on a spectrophotometer from which the luminances may be computed using the spectral power distribution of the different illuminants and the visual luminance sensitivity function. The visual luminance sensitivity function might incorporate adjustments for the appropriate light level that account for visual phenomena such as the Purkinje effect. See for instance, G. Wyszecki and W. S. Stiles, *Color Science: Concepts and Methods, Quantitative Data and Formulae*, 2<sup>nd</sup> Ed., 1982, John Wiley and Sons, Inc., New York, NY, in particular pages 406-409.

### **Simplification According to a One Illuminant/One Colorant Interaction Assumption**

[00139] Several simplifications can be incorporated into the general framework above. Suppose first, that  $N=M$  and the colorants and lights are such that colorant  $i$  absorbs only illuminant  $L_i$  and is completely transparent to all other colorants, then we have

$$\begin{aligned}
 f_i(A_1, A_2, \dots, A_M) &= \text{function of } A_i \text{ alone} \\
 &= f_i(0, 0, \dots, 0, A_i, 0, \dots, 0) \equiv g_i(A_i) \quad i=1, 2, \dots, N
 \end{aligned}$$

[00140]

(3)

[00141] The system of equations in (1) then reduces to  $M$  independent nonlinear equations one for each colorant under the corresponding illumination:



[00142] 
$$g_i(B_i) = Y_i \quad i=1,2,\dots,N$$

(4)

[00143] The achievable gamut can be defined as follows. Let:

[00144] 
$$g_i^{\min} = \min_{A_i} g_i(A_i)$$
  

$$g_i^{\max} = \max_{A_i} g_i(A_i)$$
  

$$h_i = [g_i^{\min}, g_i^{\max}] = \text{the interval of luminances from } g_i^{\min} \text{ to } g_i^{\max}$$

[00145] where  $i=1,2,\dots,N$

(5)

[00146]  $G_1$  = achievable gamut under assumption of one illuminant  
interacting with only one colorant =  $h_1 \times h_2 \times \dots \times h_N$

(6)

[00147] In other words, the achievable gamut is the product set of these individual luminance intervals. Note that the assumption in Eq. (6) is that the complete interval between the max and min limits can be realized without any "gaps" which would typically be expected with physical colorants. (For a definition of a product set, see for instance, Friedman, *The Foundations of Modern Analysis*, Dover, 1982, New York, NY.)

[00148] Under the assumption of one illuminant interacting with only one colorant, the multi-illuminant imaging characterization problem reduces significantly. Instead of requiring  $N$ -dimensional LUTs only one-dimensional LUTs – one per colorant are needed. The value of each colorant may be determined by the luminance under the corresponding illumination alone.

### Alternative Simplifications

[00149] In practice, the assumption of one illuminant interacting with only one colorant does not hold for typical colorants. However, if the strongest interactions

are between the  $i$ th illuminant and the  $j$ th colorant with other interactions having a smaller magnitude, the achievable gamut is a reduced  $N$ -dimensional region that is contained in  $G_i$ . Note that the situation of using cyan, magenta, and yellow colorants with red, green, and blue lights for illumination corresponds to this case, where the cyan interacts most with red, magenta with green, and yellow with blue. Note also that the use of a black colorant that (typically) absorbs all illuminants almost equally, does not satisfy the requirement of strong interaction with only one illuminant. In practice this implies that a black colorant should be viewed as an additional colorant, i.e., if one colorant is black we should have:

[00150]  $N = \text{number of illuminants} = \text{number of images} \leq \text{number of colorants} - 1 = M - 1$

[00151] Black may, however, be used with other colorants in special situations (as is described in the examples below) and can help improve achievable gamut (i.e., improve dynamic range), simplify computation, and reduce cost.

### **Simplifications Based on Additive Density Models**

[00152] The general technique described earlier requires a measurement of the device response in the  $M$ -dimensional input space of device control values, and the final characterization may be embodied in the form of multi-dimensional LUTs with  $N$ -dimensional inputs. In several cases, the measurement and storage/computation requirements for multi-illuminant color imaging can be significantly reduced by using simple models of the output processes. One useful model is to assume that the visual densities follow an additive model, i.e.,

[00153]

$$\begin{aligned} d_i(A_1, A_2, \dots, A_M) &\equiv -\log \left( \frac{f_i(A_1, A_2, \dots, A_M)}{f_i(0, 0, \dots, 0)} \right) \\ &= -\sum_{j=1}^M \log \left( \frac{f_i(0, 0, \dots, A_j, \dots, 0)}{f_i(0, 0, \dots, 0)} \right) = -\sum_{j=1}^M d_i(A_j) \end{aligned}$$

(7)

[00154]

where

[00155]

$$d_i(A_j) \equiv -\log \left( \frac{f_i(0, 0, \dots, A_j, \dots, 0)}{f_i(0, 0, \dots, 0)} \right)$$

(8)

[00156]

(Traditionally, densities are defined as logarithms to the base 10, any other base can also be used in practice as it changes the densities only by a scale factor and does not impact any of the other mathematical development.) Note as per our convention, the control values  $\{0, 0, \dots, 0\}$  represent an blank paper substrate and therefore  $f_i(0, 0, \dots, 0)$  represents the luminance of the paper substrate under the  $i$ th illuminant, and the logarithmic terms represent paper normalized visual densities. The additive model for visual densities is motivated by the Beer-Bouguer law for transparent colorant materials and the assumption of relatively narrowband illumination, for which the additive nature of spectral density implies the approximation above is a valid one. The model also often provides a reasonable approximation for halftone media where the assumptions do not strictly hold. (For a more detailed background, see: F. Grum and C. J. Bartleson, Ed., *Optical Radiation Measurements: Color Measurement*, vol. 2, 1983, Academic Press, New York, NY or G. Sharma and H.J. Trussell, "Digital Color Imaging", *IEEE Transactions on Image Processing*, vol. 6, No. 7, pp. 901-932, July 1997.) Full computations using a spectral density model might be performed if necessary to improve the model accuracy, this would be potentially advantageous in a situation where the illuminating lights are not strictly narrowband.

[00157] The terms  $d_i(A_j) \equiv \log\left(\frac{f_i(0,0,\dots,A_j,\dots,0)}{f_i(0,0,\dots,0)}\right)$  represent the paper normalized visual density of a patch printed with the  $j$ th colorant alone and no other colorants, with the control value for the  $j$ th colorant set as  $A_j$ . Therefore the additive density model proposed above allows the determination of the visual density of any patch based on the visual density of control patches of individual colorants. This reduces significantly the number of measurements required. Measurements of "step-wedges" of the individual colorants (for which other colorants are not printed) allow one to determine the functions  $d_i(A_j)$   $i=1,2,\dots,N$ ,  $j=1,2,\dots,M$ , from which the complete device characterization function can be determined using Eq. (8).

[00158] Using the above model, the system of equations in (1) reduces to:

[00159] 
$$\sum_{j=1}^M d_i(B_j) = \log(Y_i / Y_i^0) \text{ where } Y_i^0 = f_i(0,0,\dots,0)$$

(9)

[00160] The equations in (9) represent a system of  $K$  nonlinear equations in  $M$  variables  $(B_1, B_2, \dots, B_M)$ . The functions  $d_i(A_j)$  are available from the measurements of the "step-wedges" and the above equations can be solved for the control values  $B_j$  for luminance values within the gamut  $G$ , which was defined earlier. For points outside the gamut, the equations may be solved in an approximate sense providing a (less-controlled) form of gamut mapping.

[00161] Further simplification of these equations is possible by assuming that the densities in different spectral bands are linearly related, i.e.,

[00162] 
$$d_i(C) = \alpha_i^j d_j(C) \quad i=1,2,\dots,N$$

(10)

[00163] where  $\alpha_i^j = d_i(C)/d_j(C)$  is the proportionality factor relating the visual density for the  $j$ th colorant under the  $i$ th illuminant to the visual density for the  $j$ th colorant under the  $j$ th illuminant and is assumed to be independent of the colorant value  $C$ , and  $\alpha_j^j = 1$ . Thus the convention adopted in Eq. (10) is that the density of the  $j$ th colorant under all other illuminants is referenced to its density under the  $j$ th illuminant itself, which is not strictly a requirement of our model but is chosen because it results in a simplification of the notation alternate conventions could also be equivalently used. Equation (10) is also motivated by the Beer-Bouguer law for transparent colorant materials and the assumption of relatively narrowband illuminants. (For a more detailed background, refer to: F. Grum and C. J. Bartleson, Ed., *Optical Radiation Measurements: Color Measurement*, vol. 2, 1983, Academic Press, New York, NY or G. Sharma and H.J. Trussell, "Digital Color Imaging", *IEEE Transactions on Image Processing*, vol. 6, No. 7, pp. 901-932, July 1997.) Even though a number of colorants and marking processes do not follow the Beer-Bouguer law exactly, in practice, Eq. (10) often provides a reasonably accurate empirical model for measured data and may be used for the purposes of the current invention. With the simplification of (10) the system of equations in (9) reduces to a linear system of equations:

[00164] 
$$\sum_{j=1}^M \alpha_i^j d_j(B_j) = \log(Y_i/Y_i^0) \quad i=1,2,\dots,N$$

(11)

[00165] which can be written in matrix-vector notation as

[00166] 
$$\mathbf{A} \mathbf{d} = \mathbf{t}$$

(12)

[00167] where  $A$  is the  $N \times M$  matrix whose  $ij$  th element is  $\alpha_i^j$ ,  $d$  is  $M \times 1$  the vector whose  $j$ th component is  $d_j(B_j)$  and  $t$  is the  $N \times 1$  vector whose  $i$ th component is  $\log(Y_i/Y_i^0)$ .

[00168] The system of linear equations can be solved to determine a value of  $d$ , which provides the desired luminance values under the different illuminants (corresponding to the multiplexed images). The individual components of  $d$ , i.e., the  $d_j(B_j)$  values can then be used with the visual density response for the  $j$ th colorant under the  $j$ th illuminant to determine the control value corresponding to the  $j$ th colorant, i.e.,  $B_j$ . This process is analogous to inverting a 1-D TRC. Repeating the process for each colorant provides the complete set of colorant control values required by  $\{B_j\}_{j=1}^M$  that produce the desired set of luminance values under the different illuminants.

[00169] Note that if  $N=M$ , the above set of equations has a unique solution provided  $A$  is invertible, which is normally the case for typical colorants and illuminants. The solution in this case is obtained simply by inverting the matrix  $A$ . Furthermore, if the colorants and illuminants can be ordered in correspondence, i.e., colorant  $i$  absorbs illuminant  $i$  most and the other illuminants to a lesser extent, then  $\alpha_i^j \leq \alpha_j^i = 1$ , for all  $i=1,2,\dots,N$ , i.e., the matrix  $A$  is square with the elements along the diagonal as the largest along each row, which is often desirable from a numerical stability standpoint. If  $M > N$  the system of equations will have multiple mathematical solutions, and the choice of a particular solution may be governed by additional criteria. One example of a criterion for choosing among the multiple mathematical solutions is feasibility, a feasible solution being a set of density values that can be realized with the range of colorant control values exercisable.

[00170] The model inherent in Eq. (12) can also be used to determine suitable approximations to the achievable gamut  $G$  and can be of assistance in performing gamut mapping. Typically, the density curves  $d_j(C)$  are monotonically increasing functions of the colorant control value  $C$  and the achievable range of densities for the  $j$ th colorant under the  $j$ th illuminant is between  $d_j^{\min} = d_j(0) = 0$  and  $d_j^{\max} = d_j(C_j^{\max})$ , where  $C_j^{\max}$  is the maximum control value for the  $j$ th colorant. The achievable gamut assuming the model of Eq. (12) is valid is

[00171] 
$$G_D = \text{achievable luminance gamut assuming additive densities}$$

$$= \left\{ \mathbf{y} \text{ such that there exists a } \mathbf{d} \text{ with } \mathbf{A}\mathbf{d} = \log(\mathbf{y}/\mathbf{y}^0) \text{ and } \mathbf{0} = \mathbf{d}^{\min} \leq \mathbf{d} \leq \mathbf{d}^{\max} \right\}$$
(13)

[00172] where  $\mathbf{d}^{\min}$  is an  $M \times 1$  vector whose  $j$ th component is  $d_j^{\min} = 0$ , and  $\mathbf{d}^{\max}$  is an  $M \times 1$  vector whose  $j$ th component is  $d_j^{\max}$ ,  $\mathbf{y}$  is an  $N \times 1$  vector whose  $i$ th component represents the luminance under the  $i$ th illuminant  $L_i$ , and  $\mathbf{y}^0$  is a  $N \times 1$  vector whose  $i$ th component represents the paper luminance under the  $i$ th illuminant. The inequalities, the division, and the logarithm in the right hand side of Eq. (13) are understood to be applicable on a term-by-term basis for the vectors.

[00173] The  $N$  images to be produced under the  $N$  illuminants provide a  $N$ -tuple for each pixel location corresponding to the desired luminance values at that pixel location under the  $N$  illuminants. The  $N$ -tuples corresponding to all the pixel locations must lie within the gamut  $G$  defined earlier in order for the image to be producible using the given colorants and illuminants. If images specified for multiplexing do not satisfy this constraint some form of gamut mapping is necessary.

[00174] A simple image-independent gamut mapping scheme may be defined as follows. First, ranges of luminance values under the different illuminants are

determined such that all possible values within these ranges lie within the gamut  $G$ . This is mathematically equivalent to stating that we determine a set of  $N$ -intervals  $S_i = [Y_i^{\min}, Y_i^{\max}]$ ,  $i=1,2,\dots,N$  such that the product set of these intervals is contained within the gamut  $G$ , i.e.,

$$[00175] \quad S_1 \times S_2 \times S_3 \times \dots \times S_N \subseteq G \quad (14)$$

[00176] The gamut mapping may then be performed on an image independent basis by mapping the set of requested luminance values under the  $i$ th illuminant to the interval  $S_i = [Y_i^{\min}, Y_i^{\max}]$  by some (typically monotonous) function. The interval  $S_i$  determines the luminance dynamic range achieved under the  $i$ th illuminant. Since there are typically multiple choices of the sets  $\{S_i\}_{i=1}^N$  for which Eq. (14) is valid, one method for selecting the intervals may be by using a max min optimization where we maximize the minimum dynamic range achievable. Mathematically, this approach can be described as follows: Select the sets  $\{S_i\}_{i=1}^N$  such that  $\min_i f(S_i)$  is maximized, where  $f(S_i)$  is some suitably chosen function that measures the contrast achieved corresponding to the luminance range  $S_i$ . Examples of suitable choices of the function  $f()$  are simple luminance ratio i.e.,  $f(S_i) = Y_i^{\max} / Y_i^{\min}$ , or density range  $f(S_i) = \log(Y_i^{\max} / Y_i^{\min})$ , or CIE lightness range  $f(S_i) = L^*(Y_i^{\max}) - L^*(Y_i^{\min})$ , where  $L^*$  is the CIE lightness function. (See for instance, G. Wyszecki and W. S. Stiles, *Color Science: Concepts and Methods, Quantitative Data and Formulae*, 2<sup>nd</sup> Ed., 1982, John Wiley and Sons, Inc., New York, NY.) Note that the choice of the density range as the function in the max-min optimization along with the model of Eq.(13) reduces this to a linear max-min optimization problem with box constraints that can be solved using numerical optimization schemes.



### **Illuminant-neutral Gray Component R placement (GCR)**

[00177]           Whereas a conventional GCR technique uses common density of colorants under a single illuminant (typically ambient white light), a novel form of GCR is contemplated for the encoding and rendering of a composite image, which is described herein as "illuminant-neutral gray component replacement (GCR)", which includes determination of the common density of the colorants used in rendering the composite image, when the rendered composite images are subjected to one or more of the complementary illuminants. This specialized consideration of common density is described herein as the "cross-illuminant-common density".

[00178]           Accordingly, this illuminant-neutral GCR technique may be implemented with respect to the locations of deposited colorants in a rendered composite image that will appear dark when subjected to each of the complementary illuminants for which the composite image is encoded and rendered. For example, black can be used to replace a portion of the cyan colorant deposited in the areas of the common darkness that appear under red light; black can be used to replace a portion of the yellow colorant deposited in the areas of common darkness that appear under blue light. As a result, the common areas of darkness become more perceptible under broadband light conditions.

[00179]           For example, consider a composite image that has been encoded and rendered according to cyan and yellow separation images. Black can be used to replace a portion of the common density of cyan for recovery of a source image under red light, and black can be used to replace a portion of the common density of yellow for recovery of a source image under blue light. Common image density produced with this black component is more perceptible under white light than the same image features rendered only with cyan and yellow.

[00180] Using the cyan/yellow colorants in the above example, the white light illumination problem may be written as :

$$[00181] \quad d^W(x, y) = d_C^W(x, y) + d_Y^W(x, y) \approx d_C^W(x, y) \quad (15)$$

[00182] Cyan has a much higher density under white light compared to the density of yellow under white light, so the cyan image may be understood to dominate the appearance of a rendered composite image under white light.

[00183] Continuing with the cyan/yellow colorant example, one may select a fractional (frac) amount of common density that will be used for black (K) addition and for cyan and yellow (C, Y) subtraction. Assume a printer linearized in density, the amount of colorant, and the density of the colorant under the complementary illuminant, in a synonymous fashion. Let :

$$[00184] \quad d_K(x, y) = \text{frac} * \min [d_C^R(x, y), d_Y^B(x, y)] \quad (16)$$

[00185] This amount of density will be subtracted from  $d_C^R$  to yield  $d_C^R\text{-GCR}$ , and from  $d_Y^B$  to yield  $d_Y^B\text{-GCR}$  and the K separation will be added to the composite image. To the first-order, the density of the perceived images are as follows:

$$[00186] \quad d^R(x, y) = d_C^R\text{-GCR}(x, y) + d_Y^R\text{-GCR}(x, y) + d_K(x, y) \approx d_C^R\text{-GCR}(x, y) + d_K(x, y) = d_C^R(x, y) \quad (17)$$

$$[00187] \quad d^B(x, y) = d_C^B\text{-GCR}(x, y) + d_Y^B\text{-GCR}(x, y) + d_K(x, y) \approx d_Y^B\text{-GCR}(x, y) + d_K(x, y) = d_Y^B(x, y) \quad (18)$$

$$[00188] \quad d^W(x, y) = d_C^W\text{-GCR}(x, y) + d_Y^W\text{-GCR}(x, y) + d_K(x, y) \approx d_C^W\text{-GCR}(x, y) + d_K(x, y) \quad (19)$$

[00189] Note that under white light, a fraction of the cross-illuminant-common density  $d_K$ , now appears. This additional component yields a white light image that appears more confusing than the image described by Eq. (15). The composite image used in the generation of the rendered composite image in Figure 7 was repeated in generating the rendered composite image shown in Figure 8 with 80%

GCR (frac = 0.8). Figure 8 illustrates that the density under white light differs more from the red light density image in the GCR image compared to the non-GCR image illustrated in Figure 7. In addition to this density effect, a composite image encoded and rendered with the illuminant-neutral GCR described herein can exhibit an additional hue effect that is not illustrated in Figures 7 and 8. That is, under white light, certain regions of the rendered composite image having different amounts of cyan, yellow, and black may also exhibit different hues, thus adding to the confusion. A composite image encoded and rendered using this GCR method will be discussed in Example 1 below.

[00190]           A colorant will absorb some light from a non-complementary illuminant, and thus it will be somewhat discernible under that illuminant. To effectively suppress this appearance of a residual image, one may calibrate the perceived density for each colorant and illuminant, and one may encode the source images so as to compensate for such spurious absorption.

[00191]           Under monochromatic illumination, all colorants, neutral and non-neutral, lead to a neutral perception of density. That is, under sufficiently narrowband illumination, such as red light, an image is perceived as neutral, possessing only a varying degree of darkness, and lacking other color attributes such as hue and chroma. This perception is independent of the colorants employed to construct the image. Gray component replacement in this setting may be accomplished by replacing a given colorant with neutral colorants, non-neutral colorants, or a combination of a plurality of neutral and non-neutral colorants. The neutrality of the replacement colorant is highly illuminant dependant and we refer to GCR using a colorant that is non-neutral under white light and neutral under the target illuminant as illuminant-neutral GCR.

[00192]           Using the cyan, yellow example described above, M can be used to replace the common darkness, rather than using K as the replacement colorant. M replacement has a strong white light effect because M has relatively low

density under C and R, so a large amount of M is needed to replace the common darkness compared to the amount of K that would be needed to replace that darkness. Common densities of image features produced with this M component are more perceptible under white light than those features produced with only C and Y, or with K-based GCR. Performing illuminant-neutral GCR provides a more confused appearance under white light. Further, the GCR fraction and K and non-neutral colorant replacement can be modulated spatially to add additional confusion or to encode a third low resolution image for white light viewing.

[00193] Analytically, the process for generating an image possessing illuminant-neutral GCR can be described in a manner that is analogous to K-based GCR. Assume that the colorant values are normalized between 0 and 1 and assumed to be linear in density for both wanted and unwanted absorptions. Also assume that the maximum density of each colorant under its complementary illuminant is equal and normalized to 1. These assumptions are for purposes of simplifying the discussion and are not limitations of the general colorant-based GCR method. To teach the methodology by example, consider an illuminant-neutral GCR method that employs magenta as the replacement colorant. Let  $D_M^R$  and  $D_M^B$  be the normalized density of M under R and B illumination, respectively. In traditional color printing, these terms would be considered the unwanted absorption of M. In the present invention, that unwanted absorption will be used in a manner similar to the absorption of K in a GCR scheme.

[00194] To replace  $d_C^R(x, y)$  with magenta, the fractional amount of magenta required is  $d_C^R(x, y)/D_M^R$ . Similarly, to replace  $d_Y^B(x, y)$  with magenta the fraction of magenta required is  $d_Y^B(x, y)/D_M^B$ . The coefficients weren't needed for K-based GCR because the maximum density of K was approximately equal under the different illuminants. The largest fractional amount of magenta you can use is therefore the min of these two values.

[00195] 
$$A_M(x, y) = \min(d_C^R(x, y)/D_M^R, d_Y^B(x, y)/D_M^B, 1) \quad (20)$$

[00196] The actual amount used could be any fraction of  $A_M$

$$[00197] \quad a_M(x, y) = \text{frac} \times A_M(x, y) \quad (21)$$

[00198] The density to be subtracted from cyan and yellow can be determined given the amount of magenta colorant to be added. The subtraction for cyan and yellow is the contribution that the  $a_M(x, y)$  fraction of magenta makes towards density under red and blue illumination, respectively

$$[00199] \quad d_M^R(x, y) = a_M(x, y) D_M^R \quad (22)$$

$$[00200] \quad d_M^B(x, y) = a_M(x, y) D_M^B \quad (23)$$

[00201] An M separation is added to the image according to  $a_M(x, y)$ . The amount of density  $a_M(x, y) D_M^R$  is subtracted from  $d_C^R$  to yield  $d_C^R - \text{MGCR}$ , and  $a_M(x, y) D_M^B$  is subtracted from  $d_Y^B$  to yield  $d_Y^B - \text{MGCR}$ . To first-order, the density of the perceived images is as follows:

$$[00202] \quad d^R(x, y) = d_C^R - \text{MGCR}(x, y) + d_Y^R - \text{MGCR}(x, y) + a_M(x, y) D_M^R$$

$$[00203] \quad \approx d_C^R - \text{MGCR}(x, y) + a_M(x, y) D_M^R = d_C^R(x, y) \quad (\text{Image 1}) \quad (24)$$

$$[00204] \quad d^B(x, y) = d_C^B - \text{MGCR}(x, y) + d_Y^B - \text{MGCR}(x, y) + a_M(x, y) D_M^B$$

$$[00205] \quad \approx d_Y^B - \text{MGCR}(x, y) + a_M(x, y) D_M^B = d_Y^B(x, y) \quad (\text{Image 2}) \quad (25)$$

$$[00206] \quad d^W(x, y) = d_C^W - \text{MGCR}(x, y) + d_Y^W - \text{MGCR}(x, y) + d_M^W(x, y)$$

$$[00207] \quad \approx d_C^W - \text{MGCR}(x, y) + d_M^W(x, y) \quad (\text{Image 1} + \text{features of Image 2}) \quad (26)$$

[00208] The term  $d_M^W(x, y)$  is much larger than  $d_K(x, y)$  of the K-based GCR method [Eq. (19)] because  $d_M^W$  is scaled by  $1/ D_M^R$  or  $1/ D_M^B$ , which are both much larger than 1 due to the normalized unwanted absorption densities being much less than 1. The large  $d_M^W(x, y)$  indicates that the features of image 2 will

be represented with higher density than in the K-based GCR case. More image confusion or more capacity to encode a third white light effect can be achieved using this higher range of density for the white light interaction. An example of this encode will be shown below. To encode and render an additional, low-resolution source image by use of a magenta (M) colorant the fractional GCR component  $\text{frac}$  is given a spatial dependence according to the additional low-resolution source image. Example 3, below, includes such a low-resolution image encoded according to the fraction of GCR that is applied.

[00209] In addition to increased density capacity of the white light interaction, there is an additional hue introduced into the white light image when using the M-based GCR method. The introduced M component creates another dimension in color space to yield a wider range of hues in the white light image as compared to the range of hue achieved in the K-based GCR method. Further, the M-based and K-based GCR methods may be combined and used in conjunction at one spatial location or alternated in a controlled manner across  $(x, y)$ . Use of both methods further increases the capacity to create interesting white light effects, such as for embedding an additional pattern that is revealed under a multiband illuminant or a wideband illuminant such as white light.

[00210] The above example used cyan and yellow to primarily encode source images and magenta was used for density replacement. It is readily apparent that other combinations of colorants can be used for primary encoding of images and for density replacement. In fact, multiple non-neutral colorants can be used for density replacement. The example below describes one monochromatic constructed of multiple colorants.

[00211] Consider another aspect of the present invention, where, for example, one monochromatic image is constructed of common colorants (subtractive primaries - C, M, Y, K), is designed to be observable under red illumination and

possess density distribution  $d^R(x, y)$ . To produce that print, the colorants can be used in any combination that satisfies the sum

[00212] 
$$d^R(x, y) = d_C^R(x, y) + d_M^R(x, y) + d_Y^R(x, y) + d_K^R(x, y),$$
  
(27)

[00213] where the red densities of the colorants are used in the sum. In this setting, only one image is present, and "common density" available for GCR replacement reduces to the density of the image and the relative amounts of C, M, Y, and K can be varied spatially to produce prints with desirable properties under different illuminants. For example, the image may be composed of squares, where only one colorant is used in a given square. The squares may be randomly arrayed or arranged in some desired pattern. Under white illumination, a multicolored pattern would be observed that has a range of hues determined by the chosen C, M, Y, K pattern. In general, mixes of colorants and colorants beyond the common subtractive primaries may be used in a wide variety of spatial patterns.

[00214] Note that the unwanted absorption of colorants will be used, and for a given colorant that absorption can be relatively low compared to the absorption for the colorant that is complementary to the illuminant (for example, cyan colorant is complementary to red illumination). In some spatial locations of an image, the desired density may be higher than the density of the unwanted absorption of a single non-complementary colorant. For example, yellow has low density under red illumination and a maximum amount of yellow may not provide sufficient density for some high density locations of an image. In that case, multiple colorants must be used at that location, or the overall density range of the image must be reduced.

[00215] The above description was simplified to aid in teaching the basic concept. There are other considerations that are taken into account to achieve good image quality. A notable consideration is that a given colorant can absorb

some light from a non-complementary illuminant, thus it will not completely disappear under that illuminant. To effectively suppress the appearance, one may calibrate the perceived density for each colorant and illuminant and construct separation images to compensate for the spurious absorption. Much of this generalized theory has been described above. Also note that the above description used conventional subtractive primaries to encode the images. Other colorants could be used and to achieve optimal results, calibration under the appropriate illuminants and accounting for the spurious absorption is advantageous. Additional practical considerations may also be applicable. For instance, the linear response in density for absorptions under different narrowband illuminants may not provide an accurate enough approximation and the actual nonlinearity of the responses may be corrected through a correction process following the principles outlined above, but using more general techniques such as look-up-tables or neural networks.

### **Illustrated Embodiments of the Invention**

[00216] For a general understanding of the present invention, reference is made to the drawings. In the drawings, like reference numerals have been used throughout to designate identical elements.

[00217] Figure 3 illustrates a system 100 operable in a first mode for spectrally multiplexing a plurality of source images to form a composite image, in a second mode for rendering the composite image, or in a third mode for demultiplexing the spectrally multiplexed composite image so as to recover at least one of the plurality of source images for advantageous viewing by an observer.

[00218] As shown in Figure 3, a plurality of disparate source image arrays 11-1, 11-2, ...11-N are presented to an image input device 20 in a spectral multiplexing system 101. Image input device 20 may be equipped to receive plural monochromatic images or a combination of monochromatic and polychromatic



images. Image input device 20 may include an image capture device such as a digital scanner coupled to a random access memory, or any type of analog or digital camera coupled to a storage means such as a computer memory or a magnetic or optical recording medium. Image input device 20 may also include means for receiving an image that had previously been stored in a random access memory, on video tape, or a laser-encoded disk, etc., or for receiving an image created by a computer image generator, or an image encoded in an appropriate format and transmitted on a network.

[00219] The illustrative representation of the plural source images in respective image arrays received by the image input device 20 in this example includes a first source image 12-1 represented in a first source image array 11-1 and a second source image 12-2 represented in a second source image array 11-2. The system 101 can optionally receive  $N$  source images which are represented in a respective image arrays. In this exemplary embodiment of the invention, disparate pictorial source images are employed and at least one of the plural source images is intended for ultimate recovery (via spectral demultiplexing) from a composite image.

[00220] Once the source image data is received in the input image device 20, it is presented to a spectral multiplexer 30, which encodes a data representation of a composite of at least the first and second source images, so as to provide a composite image 32 on an spectrally multiplexed (SM) image plane. Such encoding may proceed in one embodiment with mapping for every pixel location, or by mapping in localized areas rather than specific pixels, to the composite image 32, so as to multiplex the information necessary for encoding of each corresponding pixel located in each source image.

[00221] Next, according to operation of a composite image rendering system 102, data representative of the composite image is provided to a rendering device 40, which can be connected to the spectral multiplexer 30 by any one of a variety

of suitable means for transmitting or storing electronic information. The rendering device 40 records the composite image 32 on a substrate 44 with use of a predetermined array of narrowband colorants, so as to form a rendered composite image 42. The rendered composite image 42 is thereby fixed on the substrate 44.

[00222] The rendered composite image 42 is available to an observer 70 for viewing in ambient light. Although the rendered composite image 42 is representative of data encoded in the spectrally multiplexed plane using the method of the invention, the rendered composite image 42 typically exhibits a confused appearance under conventional ambient lighting conditions; at least one of the source images 12-1, 12-2, etc. is thus difficult or impossible to distinguish under conventional ambient lighting conditions. A particular source image is made difficult or impossible to distinguish until a demultiplexer 50 is operated to selectively illuminate the composite image 42 in a manner sufficient to reveal the desired source image. Alternatively, one or more of the source images may be encoded so as *avoid* visual confusion and therefore be visually apparent in the rendered composite image when the rendered composite image is subjected to conventional ambient lighting conditions, and become confused or difficult to detect when the rendered composite image is subjected to a complementary narrowband illuminant.

[00223] According to operation of a spectral demultiplexing system 103, a particular source image (as shown in Figure 3, source image 12-1) may be recovered and made distinguishable within the composite image 42. In the embodiment illustrated in Figure 3, the output of the demultiplexer 50 is directed to an observer 70 using the method of the invention. The recovered image is then distinguishable by the observer 70 as one substantially identical with, or a close approximation of, the particular source image 12-1 initially provided to the image input device 20.

[00224] Recovery of a particular source image will be understood to generally proceed according to an exemplary embodiment of the spectral demultiplexing system 103 as follows. The substrate 44 is positioned with respect to an illuminant source operable within the demultiplexer 50, such that a selected illuminant generated by the demultiplexer 50 illuminates the composite image 42 so as to subject the array of colorants in the rendered composite image 42 to the predefined spectral power distribution of the selected illuminant. As a result of the rendered composite image 42 thus being controllably and selectively illuminated by a selected illuminant, a desired source image is then made visually distinguishable to an observer 70. The desired source image 12-1, now recovered, is thereby susceptible to comprehension by the observer 70.

[00225] Accordingly, by virtue of the aforementioned interaction of one or more colorants and their complementary illuminants, and due to the visual response of the observer 70 to this particular interaction, each encoded source image may or may not be distinguishable during spectral demultiplexing depending upon the objective of the demultiplexing operation.

[00226] Figure 4 is a simplified schematic diagram of exemplary embodiments of spectral multiplexing, rendering, and spectral demultiplexing methods 61, 62, 63, respectively. In step 61 for multiplexing plural source images, image data representing a source image in a first separation image 71 and a second separation image 72 are provided to the multiplexer 30, which outputs a composite image data file to a rendering device 40. The output of the rendering device 40 is substrate 90 which has incorporated therein a composite image 92. The separation image 71 is rendered as a pattern using a first colorant; in the illustrated embodiment, a cyan ink or toner is chosen. The second separation image 72 is rendered as a pattern using a second colorant; in the illustrated embodiment, a magenta ink or toner is chosen. (As there is typically some overlap in absorption bands between practical narrowband colorants, the two separation

images are preferably encoded in step 61 to account for the absorption that will occur when plural colorants are utilized to produce the composite image.)

[00227] In a rendering step 62, the composite image specifies patterns in cyan and magenta colorants that are accordingly rendered on a substrate 90 to form the rendered composite image 92. Those skilled in the art will appreciate that certain portions of the two patterns may be co-located and other portions are relatively spatially distinct. Nonetheless, in certain embodiments of the present invention that utilize plural source images, visual recognition of at least one of the plural source images encoded in the composite image may be made difficult or impossible due to the confusion between colorant patterns in the composite image.

[00228] In step 63 for demultiplexing the rendered composite image 92, the substrate 90 having the rendered composite image 92 fixed thereon is illuminated by the demultiplexer 50. Controlled illumination of the substrate 90 according to a first mode 51 of illumination causes the first separation image 71 to achieve a particular level of density with respect to the remainder of the composite image and thus the first separation image 71 becomes detectable on the substrate 90. Controlled illumination of the substrate 90 according to a second mode 52 of illumination causes the second separation image 72 to be similarly detectable on the substrate 90. In the illustrated embodiments, the first source image 71 and the second source image 72 are therefore selectably distinguishable on the substrate 90. Controlled illumination of the substrate 90 according to simultaneous operation of first and second modes 51, 52 thereby causes both the first separation image 71 and the second separation image 72 to be distinguishable.

[00229] Figure 5 illustrates a schematic simplified representation of the spectral multiplexing system 101 of Figure 3, in which an image processing unit 130 and associated peripheral devices and subsystems are employed. An image input terminal 120 may include an image capture device 122 such as a scanner, digital

camera, or image sensor array; a computer image generator 124 or similar device that converts 2-D data to an image; or an image storage device 126 such as a semiconductor memory or a magnetic, optical, or magneto-optical data storage device. The image input terminal 120 derives or delivers digital image data in the form of, for example, plural monochromatic image files, wherein the picture elements or "pixels" of each image are defined at some gray value. For example, the input terminal 120 may be employed to derive an electronic representation of, for example a document or photograph from image capture device 122, in a format related to the physical characteristics of the device, and commonly with pixels defined at  $m$  bits per pixel. If a color document, the image is defined with two or more separation bitmaps, usually with identical resolution and pixel depth. Image data from the input terminal 120 is directed to an image processing unit (IPU) 130 for processing so as to be encoded to create a composite image. It will be recognized that the data representing one or more source images is spectrally encoded by the image processing unit 130 to provide secondary image data representative of a composite image suitable for subsequent rendering.

[00230] The image processing unit 130 may include image memory 132 which receives input image data from image input terminal 120 or from another suitable image data source, such as an appropriately programmed general purpose computer (not shown) and stores the input image data in suitable devices such as random access memory (RAM). Image processing unit 130 commonly includes processor 134. The input image data may be processed via a processor 134 to provide image data representative of plural source images defined on respective source image planes in accordance with the present invention. For example, image data signals in the form of RGB or black and white (B/W) images may be processed, and the luminance information derived therefrom may be used to provide data representative of a source image. Image data signals presented in other formats are similarly processed: image data signals in, for example the

L\*a\*b format, may be processed to obtain data representing a source image from the lightness channel. Image data signals that are already formatted in grayscale are generally usable without further processing.

[00231] Operation of the image processing unit 130 may proceed according to one or more image processing functions 138, 139 so as to encode the source image data into the composite image file as described hereinabove. Processing may include a color conversion which, if necessary, may be implemented to convert a three component color description to the printer-specific four or more component color description, and may include a halftoner which converts a *c* bit digital image signals to *d* bit digital image signals, suitable for driving a particular printer, where *c* and *d* are integer values. In certain embodiments, additional functions may include one or more of color space transformation, color correction, gamut mapping, and under color removal (UCR)/gray component replacement (GCR) functions. Control signals and composite image output data are provided to an interface 136 for output from the image processing unit 130.

[00232] The image processing unit 130 may be embodied as an embedded processor, or as part of a general purpose computer. It may include special purpose hardware such as for accomplishing digital signal processing, or merely represent appropriate programs running on a general purpose computer. It may also represent one or more special purpose programs running on a remote computer.

[00233] Figure 6 is a simplified schematic representation of the spectral demultiplexing system 103 of Figure 3, in which a controller and associated peripheral devices and subsystems are employed to obtain one or more recovered source images 171, 172. Figure 6 shows a controller 150 connected to an illuminant source 160 that is operable for subjecting the composite image 42 on substrate 44 to at least one of first and second predefined illuminants 161, 162. Firstly, as illustrated with reference to the rendered composite image 42 on

substrate 44, under conventional ambient lighting and in the absence of illuminants 161, 162; only the composite image 42 is distinguishable and no source image is easily detected. However, upon activation of the source 160 so as to provide the first predefined illuminant 161, the recovered source image 171 becomes detectable to an observer 170. Alternatively, the mode of operation of the source 160 may be switched so as to provide a second predefined illuminant 162, whereupon the composite image 42 is instead subjected to the second illuminant 162, and the recovered source image 172 becomes detectable.

[00234] The controller 150 may be constructed as in the form of a manually-operable illuminant selector switch. Alternatively, as illustrated, the controller 150 may be provided in the form of a computer-based control device having an interface 156 connected to source 160, which offers programmable control of the operation of the illuminant source 160. The controller 150 may thus be operated to cause selective activation and deactivation of the illuminant source 160 so as to provide one or more selected fields of illumination 162. Such control may, for example, be accomplished via manual operation of the illuminant source 160 by a human operator, or by programmable control afforded by a computer or similar means.

[00235] The controller 150 is operable for accomplishing tasks such as activation, deactivation, or sequencing of the illuminant source 160, setting illuminant intensity, illuminant frequency, etc.. Embodiments of the controller 150 benefit from operation of a programmable control system comprising standard memory 152 and processor 154. The controller 150 may be employed, for example, for supplying uniform R or G or B screen images to the interface 156 for subsequent display on the illuminant source 160 when the latter is constructed in the form of a CRT monitor.

[00236] Operation of the illuminant source 160 by the controller 150 may proceed according to certain sequenced control functions so as to provide, for

example, controlled operation of the illuminant source 160 to afford a field of illumination that varies according to selective characteristics such as: sequential or simultaneous activation and deactivation of selected illuminants, each having a predefined spectral power distribution; controlled variation of the intensity of selected illuminants; or for interactive control according to intervention by an operator of the particular sequence, intensity, or duration of the illuminants. As noted above, the rendered composite image may be constructed to have a plurality of source images encoded therein; for example, of at least first and second patterns of respective first and second colorants. The rendered composite image may be subjected to a temporal sequencing of illumination by respective first and second narrowband illuminants, thus allowing a respective one of the first and second recovered source images 171, 172 to be sequentially distinguishable.

[00237] As mentioned, the illuminant source 160 may be provided in the form of a CRT monitor having a screen positionable with respect to the substrate 44 for generating the requisite field of illumination sufficient to illuminate the rendered composite image 42.

#### **Examples of rendered composite images generated using the illuminant-neutral GCR technique**

[00238] *Example 1: Illuminant-neutral GCR as applied to C/Y encoded images*

[00239] Figure 9 is a rendered composite image wherein two source images are encoded and rendered in cyan and yellow colorants that are respectively designed for viewing under red and blue illumination. The rendered composite image incorporates a small amount of black (K) to compensate for unwanted absorptions by cyan (C) (so as to make the cyan image less than discernible under illumination in the blue region and to recover the source image in the presence of a yellow illuminant). The use of K greatly increases the dynamic range available for encoding the source images. Note that when this rendered



composite image is viewed under white light, the image in cyan (C) dominates the other confused images and the source image encoded in yellow (Y) is hardly visible.

[00240] Figure 10 is a rendered composite image created with a 80% GCR fraction, wherein the appearance of the rendered composite image under red and blue illumination is substantially similar to the appearance of the rendered composite image provided in Figure 9, but the rendered composite image in Figure 10 under white light is more confused due to the application of GCR.

[00241] Figure 11 is a rendered composite image created with illuminant-neutral GCR using magenta as the replacement colorant, wherein the appearance of the rendered composite image under red and blue illumination is substantially identical to the appearance of the rendered composite image provided in Figure 9, but the rendered composite image in Figure 11 appears under white light as more confused than that of Figures 9 and 10 due to the application of illuminant-neutral GCR.

[00242] *Example 2: Use of spatially-varying illuminant-neutral GCR for encoding an additional source image*

[00243] Figure 12 is a composite image having encoded therein first and second source images intended for recovery under blue and red illumination wherein illuminant-neutral GCR has been utilized in the rendering of the composite image in cyan and yellow colorants, and having a third source image encoded therein for recovery under white light illumination. The amount of illuminant-neutral GCR is spatially varied in accordance with the image content of the third source image. In the rendered composite image of Figure 12, the image content of the third source image is a binary pattern in the shape of the "digital X" (a trademark of Xerox Corporation), with use of a M-based GCR in the regions of the composite image that correspond to the image content of the third source image, and no GCR being implemented in the remaining regions of the composite

image. When the image is subjected to red or blue light, a respective one of the first and second source images is recovered. Under white light, the third source image is discernible.

[00244] In alternative embodiments, the contemplated third source image may include or be restricted to image content that is encoded for detection primarily or exclusively by automated instrumentation (i.e. image content that is encoded to be machine-readable rather than human-readable).

[00245] In still other embodiments, the third source image may be encoded as a grayscale image by use of a suitable halftoning technique.

[00246] *Example 3: Varying illuminant-neutral GCR for optimized confusion*

[00247] Figure 13 is a rendered composite image that exemplifies an additional application of the contemplated illuminant-neutral GCR technique, wherein the M-based GCR was applied over the randomly-positioned square blocks of pixels. Note that the resulting rendered composite image will reveal the encoded source images under illumination by red and blue illuminants but image confusion is evident in the rendered composite image when subjected to white light. The level of image confusion may be further optimized by choosing the image alignments with respect to the particular application of the illuminant-neutral GCR technique. The image confusion may be increased when the frequency content of the illuminant-neutral GCR matches that of the dominant image and the dark regions in the two encoded images align so as to allow a selected amount of variation in illuminant-neutral GCR.

[00248] *Example 4: Illuminant-neutral GCR for single monochromatic image*

[00249] Figure 14 is a rendered composite image that exemplifies illuminant-neutral GCR implemented using multiple colorants and a single monochromatic image intended for viewing under blue illumination. The colorant selected for darkness replacement was varied randomly square-to-square over 6 mm squares.

In this example, cyan, magenta, yellow, and black were used independently in image locations where they could provide sufficient density under blue light. Areas that required more density than cyan, magenta, or yellow could provide were supplemented with black colorant. In varying the replacement color, a variety of spatial patterns may be used wherein the patterns are independent of the image, such as the illustrated square-to-square variation, or the patterns can be correlated to image features, whereby defined segments of a subject (such as a face) are rendered with use of a particular color.

[00250] Note that one skilled in the art may realize a variety of alternatives are within the scope of this invention for implementing the above described embodiments. Its advantageous use is expected in color printing by various processes including offset lithography, letterpress, gravure, xerography, photography, and any other color reproduction process which uses a defined number of colorants, usually three or four, in various mixtures. Embodiments of the rendering system 102 include apparatus capable of depositing or integrating a defined array of colorants in a substrate, according to the composite image, such that the array of colorants is susceptible to selective reflection or transmission of a selected narrowband illuminant incident thereon. For example, the composite image may be rendered on a transparent film and a desired source image may be recovered when the substrate is backlit by a suitable narrowband illuminant. Examples include hardcopy reprographic devices such as inkjet, dye sublimation, and xerographic printers, lithographic printing systems, silk-screening systems, and photographic printing apparatus; systems for imagewise deposition of discrete quantities of a color on a substrate surface, such as paint, chemical, and film deposition systems; and systems for integration of colorant materials in an exposed surface of a substrate, such as textile printing systems.

[00251] Embodiments of exemplary substrates include, but are not limited to, materials such as paper, cardboard, and other pulp-based and printed packaging

products, glass; plastic; laminated or fibrous compositions; and textiles. Narrowband colorants other than basic CMYK colorants may also be used for this invention.

[00252] The field of illumination for illuminating a rendered composite image may be provided by a variety of illuminant sources that include a narrowband light source responsive to manual control or to program control according to an illuminant source control signal. Various narrowband light sources may include apparatus for providing filtered sunlight, filtered incandescent, or filtered fluorescent light; coherent light sources such as a solid-state laser or laser diode; projection or image display devices such as those incorporating a cathode ray tube (CRT), flat-panel display (FPD), liquid crystal display (LCD), plasma display, or light emitting diode (LED) and organic light emitting (OLED) arrays. Light sources incorporating a cathode ray tube are advantageous in that they have phosphors that exhibit stable and well-understood spectral characteristics that are sufficiently narrow and complementary to common CMY colorants. In addition, such displays are widely available.

[00253] Additional familiar components (not shown) may be included such as a keyboard, and a mouse, means for reading data storage media, a speaker for providing aural cues and other information to the observer, and adapters for connection of the systems described herein to a network medium. Computer readable media such as memory, hard disks, CD-ROMs, flash memory, and the like may be used to store a computer program including computer code that implements the control sequences pertinent to present invention. Other systems suitable for use with the present invention may include additional or fewer subsystems.

[00254] Embodiments of the invention are contemplated for providing visual stimulation and amusement, particularly by the inclusion of composite images in printed materials such as books or posters, in novelty items, and in software sold

to consumers for generating such items. Rendered composite images made using this invention can be distributed to consumers for subsequent demultiplexing when exposed to a field of illumination generated by, for example, a display device connected to a computer according to display control signals directed to the computer from a remote source, such as from an internet site, or according to display control instructions embedded in electronic mail, Internet web pages, or similar transmissions.

[00255]           Embodiments of the invention may be employed for drawing the attention of an observer to a particular source of information, such as for disseminating news, entertainment, or advertising, or to messages or indicia, such as trademarks or product instructions, on objects; to graphics, art work, and the like displayed at gathering places such cinemas, galleries, museums, commercial venues, and trade shows; or to large-format displays such as signs, posters, billboards, or murals. Still other embodiments of the invention are contemplated for use in publications, merchandising, or advertising vehicles such as newspapers, periodicals, or maps; in boxes, bottles, containers, wrappers, labels, or other packaging or shipping materials; in building materials including wall coverings, floor coverings, lighting systems, and the like.

[00256]           Other embodiments of the invention are contemplated for implementing specialized visual effects in a public setting, a performance or entertainment venue, or other gathering place where there is control of the ambient lighting. Examples are festivals, theaters, night clubs, and sporting events, where participants may receive printed materials or packaging, clothing, souvenirs, etc. having incorporated thereon one or more rendered composite images. Under the influence of localized fields of illumination provided by suitably-modified zone lighting equipment, such as stage lighting equipment, which may be synchronized or otherwise controlled, a variety of source images having visual interest to the participants may be made visible in a dramatic fashion.

[00257] Other embodiments of the invention are contemplated for implementing secure verification of authenticity of a document or other instrument. Such embedded information may be present in the form of a watermark, an indice, or an image useful for validation, secure identification, or the like. For example, the appearance of a single image or an unchanging (i.e. constant) image viewed under specific, controlled illumination could be used to indicate authenticity of a document. Fraudulent attempts to circumvent the verification, such as by proffering a photocopy or counterfeit of the requisite instrument, may not meet the printer calibration settings necessary for generating an authentic composite image, such that a confused appearance of a composite image on a counterfeit under the controlled lighting would preclude authenticity. Embodiments of the invention are contemplated for providing simple encryption and decryption of embedded information in documents, coupons, game pieces, tickets, certificates, commercial paper, currency, identification cards, and the like.

[00258] Still other embodiments of the invention are contemplated for use in textiles and garments such as head coverings, clothing, and outerwear, and in other wearable or personal items such as footwear, timepieces, eyewear, jewelry, appliques, fashion accessories, and the like. Items bearing composite images generated in the course of the practice of this invention may have an artistic, novelty, or collectible nature, such as in a souvenir, book, magazine, poster, educational material, trading card, or toy.

[00259] While particular embodiments have been described, alternatives, modifications, variations, improvements, and substantial equivalents that are or may be presently unforeseen may arise to applicants or others skilled in the art. Accordingly, the appended claims as filed and as they may be amended are intended to embrace all such alternatives, modifications variations, improvements, and substantial equivalents.